

***RC-CLASS AND LC-CLASS ON FIXED POINT  
THEOREMS FOR  $\alpha$ -CARISTI TYPE  
CONTRACTION MAPPINGS***

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**Abstract.** In this paper, we introduce the notion of  $(\alpha, \mathcal{H}_{LC}, f_{RC})$ -Caristi type contraction mappings and prove fixed point theorem by using this notion on complete metric space. To illustrate our result, we construct an example.

[Full text](#)

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