

DETERMINATION TEMPERATURE OF A HEAT EQUATION FROM THE FINAL VALUE DATA

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Abstract. We introduce the truncation method for solving a backward heat conduction problem. For this method, we give the stability analysis with new error estimates. Meanwhile, we investigate the roles of regularization parameters in these two methods. These estimates prove that our method is effective.

[Full text](#)

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