

## CHARACTERIZATION OF THE ORDER RELATION ON THE SET OF COMPLETELY $n$ -POSITIVE LINEAR MAPS BETWEEN $C^*$ -ALGEBRAS

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**Abstract.** In this paper we characterize the order relation on the set of all nondegenerate completely  $n$ -positive linear maps between  $C^*$ -algebras in terms of a self-dual Hilbert module induced by each completely  $n$ -positive linear map.

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