

ABSTRACT. An extended eigenvalue for an operator  $A$  is a scalar  $\lambda$  for which the operator equation  $AX = \lambda XA$  has a nonzero solution. Several scenarios are investigated where the existence of non-unimodular extended eigenvalues leads to invariant or hyperinvariant subspaces.