



GEOMETRIC METHODS IN QUANTUM MECHANICS

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Abstract. This is a survey on geometric quantum mechanics and some of its implications on general issues in quantum theory.

Contents

1	Introduction	2
2	Preliminary Tools	3
2.1	Some Basic Symplectic Geometric Terminology	3
2.2	Complex Polarizations and Kähler Manifolds	4
2.3	A Digression on Geometric Invariant Theory	4
2.4	Completely Integrable Hamiltonian Systems	4
2.5	A Glimpse at Geometric Quantization	5
2.6	The Bohr-Sommerfeld Condition	7
2.7	Holomorphic Geometric Quantization	7
2.8	A Hydrodynamical Intermezzo	8
3	Geometric Quantum Mechanics: the Basic Formalism	11
3.1	Projective Space and its Symplectic and Kähler Geometry	11
3.2	The Chern-Bott Connection	14
3.3	Toral Actions and Integrability	15
3.4	Uncertainty and Jacobi Fields	18
3.5	Hydrodynamical Aspects of Geometric Quantum Mechanics	19
3.6	Aharonov-Anandan Phase for Mixed States	22